

◇ 電子科学研究所学術講演会 ◇

講演者:

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Approximation Algorithms on Some Network Optimization Problems

Given a metric graph $G = (V, E, w)$, a center $c \in V$, and an integer k , the **Star k -Hub Center Problem** is to find a depth-2 spanning tree T of G rooted by c such that c has exactly k children and the diameter of T is minimized. Those children of c in T are called hubs. A similar problem called the **Single Allocation k -Hub Center Problem** is to find a spanning subgraph H^* of G such that (i) C^* is a clique of size k in H^* ; (ii) $V \setminus C^*$ forms an independent set in H^* ; (iii) each $v \in V \setminus C^*$ is adjacent to exactly one vertex in C^* ; and (iv) the diameter $D(H^*)$ is minimized. The vertices selected in C^* are called hubs and the rest of vertices are called non-hubs. Both **Star k -Hub Center Problem** and **Single Allocation k -Hub Center Problem** are NP-hard and have applications in transportation system, telecommunication system, and post mail system. In this talk, we give $5/3$ -approximation algorithms for both problems. Moreover, we prove that for any $\varepsilon > 0$, the **Star k -Hub Center Problem** has no $(1.5 - \varepsilon)$ -approximation algorithm unless $P = NP$. Under the assumption $P \neq NP$, for any $\varepsilon > 0$ the **Single Allocation k -Hub Center Problem** has no $(4/3 - \varepsilon)$ -approximation algorithm.